

**COMPLEMENTARY TRIPLE CONNECTED SUBSTANTIAL  
INDEPENDENCE NUMBER FOR THE LEXICOGRAPHIC  
PRODUCT OF PATHS AND CYCLES**

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**Abstract:** A Complementary triple connected substantial independent set is a non-empty subset  $S \subset V$  of a graph  $G = (V, E)$  if  $S$  is a substantial independent set and the induced subgraph  $\langle V - S \rangle$  is triple connected. The Complementary triple connected substantial independence number is the maximum cardinality among all Complementary triple connected substantial independent sets and is indicated by  $\beta_{ctcs}$ . In this paper, we determine the value of Complementary Triple connected substantial independence number for the lexicographic product of paths and cycles.

**Keywords and Phrases:** Independence number, Substantial independent set, Complementary triple connected substantial independent set.

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## **1. Introduction and Preliminaries**

A **substantial independent set** is a non-empty subset  $S \subset V$  in a connected graph  $G$  if  $S$  is an independent set of  $G$  and any vertex in  $V/S$  is join by an edge to atmost one vertex in  $S$ . The **substantial independence number** of  $G$  is the supremum cardinality among all substantial independent sets in  $G$  and is indicated